

# Mecanismos

## Prof. Jorge Luiz Erthal

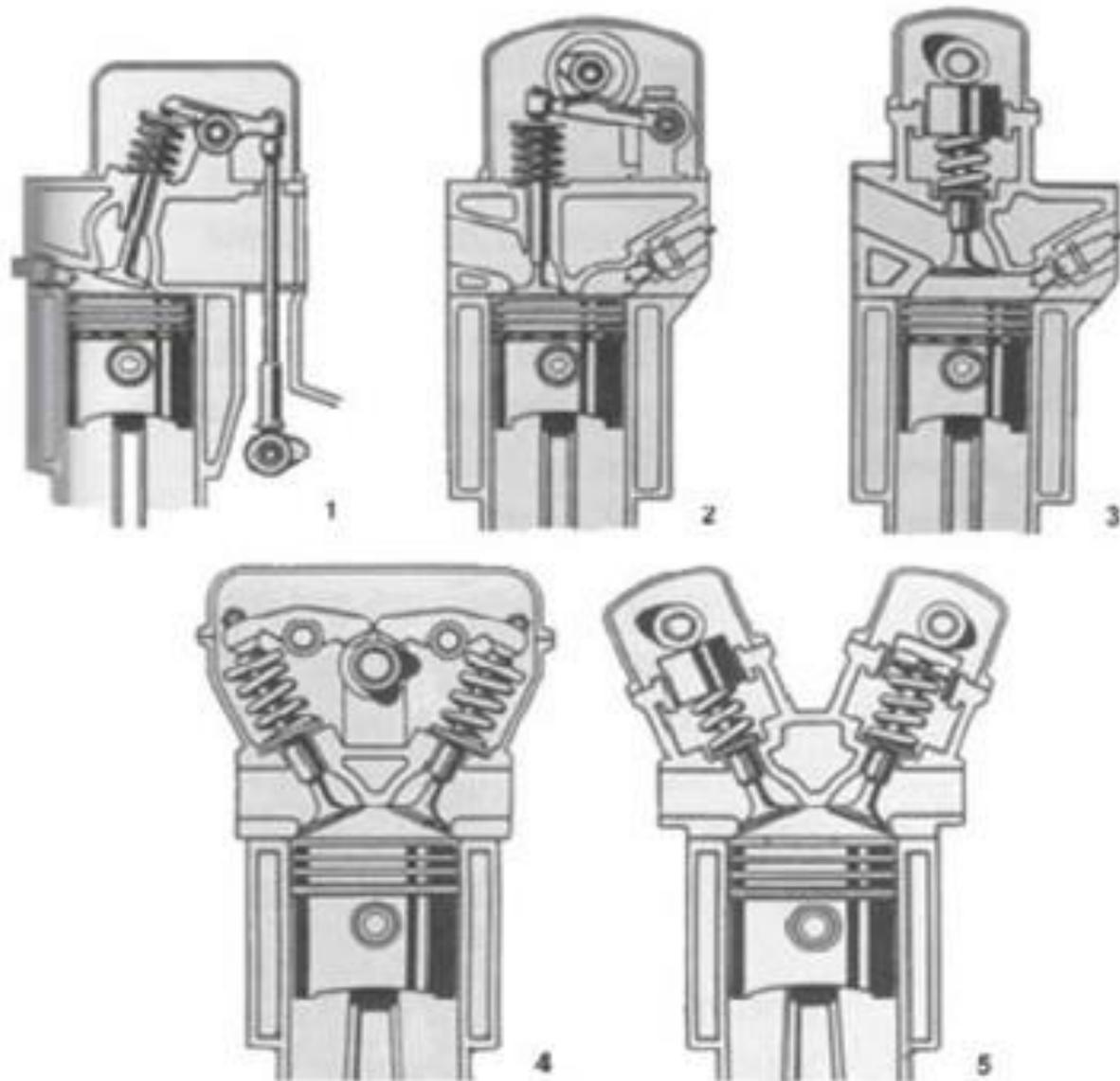
jorgeerthal@gmail.com

### Síntese de cames com seguidor oscilante

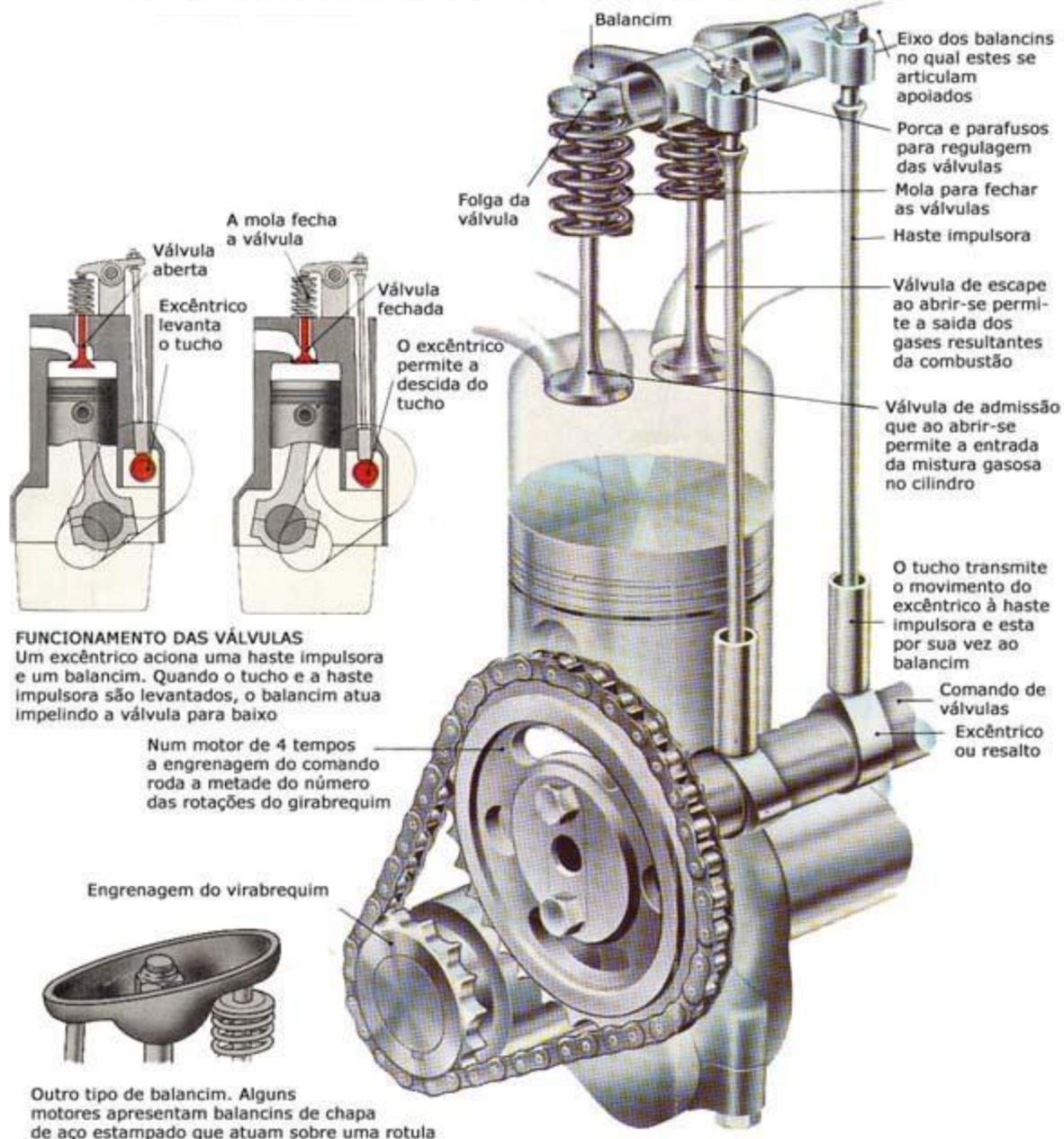
# Nesta aula

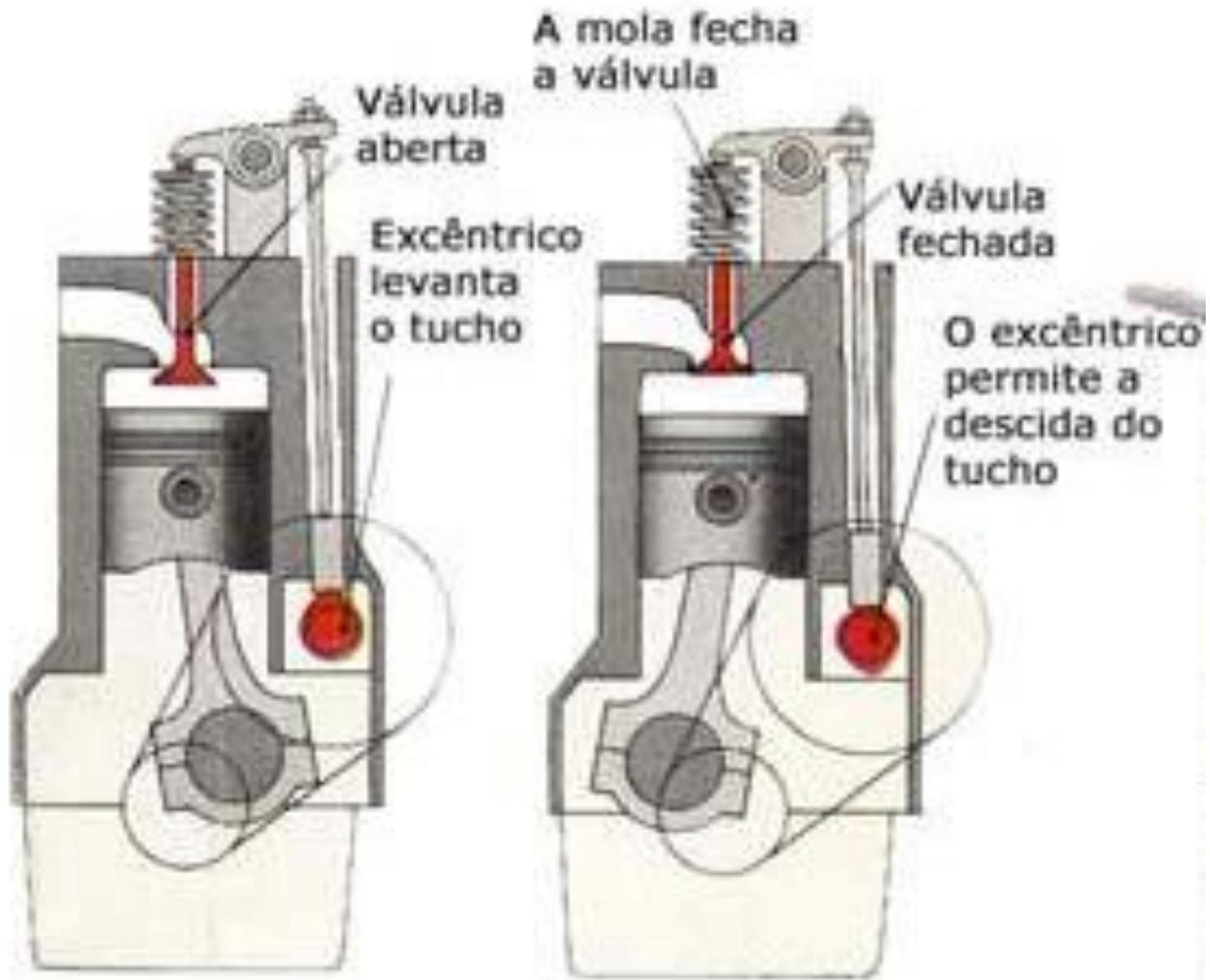
- Síntese de came com seguidor oscilante de face plana
  - Largura da face do seguidor
  - Coordenadas do perfil da came
  - Raio de curvatura
- Síntese de came com seguidor oscilante com rolete
  - Coordenadas do perfil da came
  - Orientação da linha de contato
  - Raio de curvatura

## DIFERENTES TIPOS DE ACCIONAMIENTO DE VALVULAS

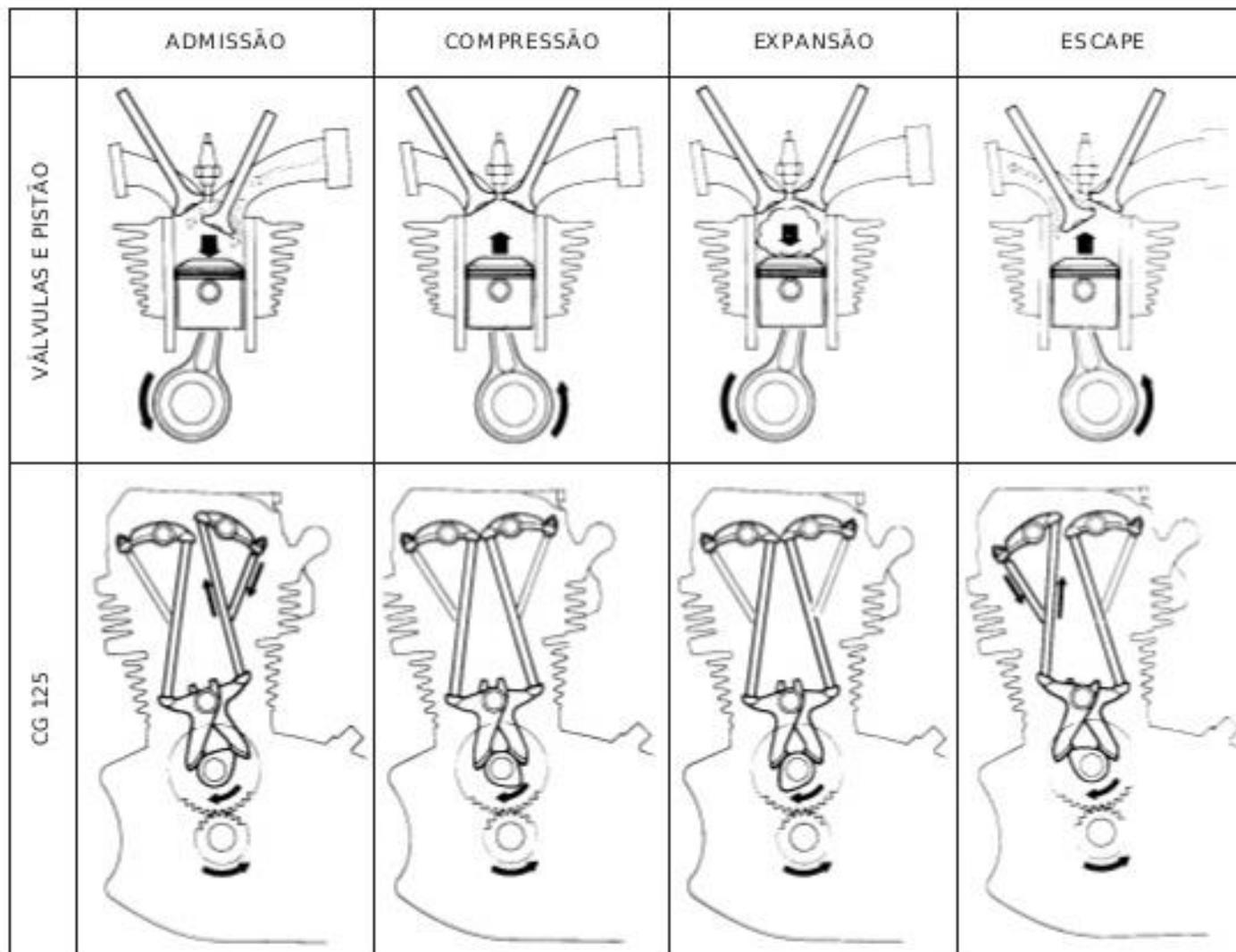


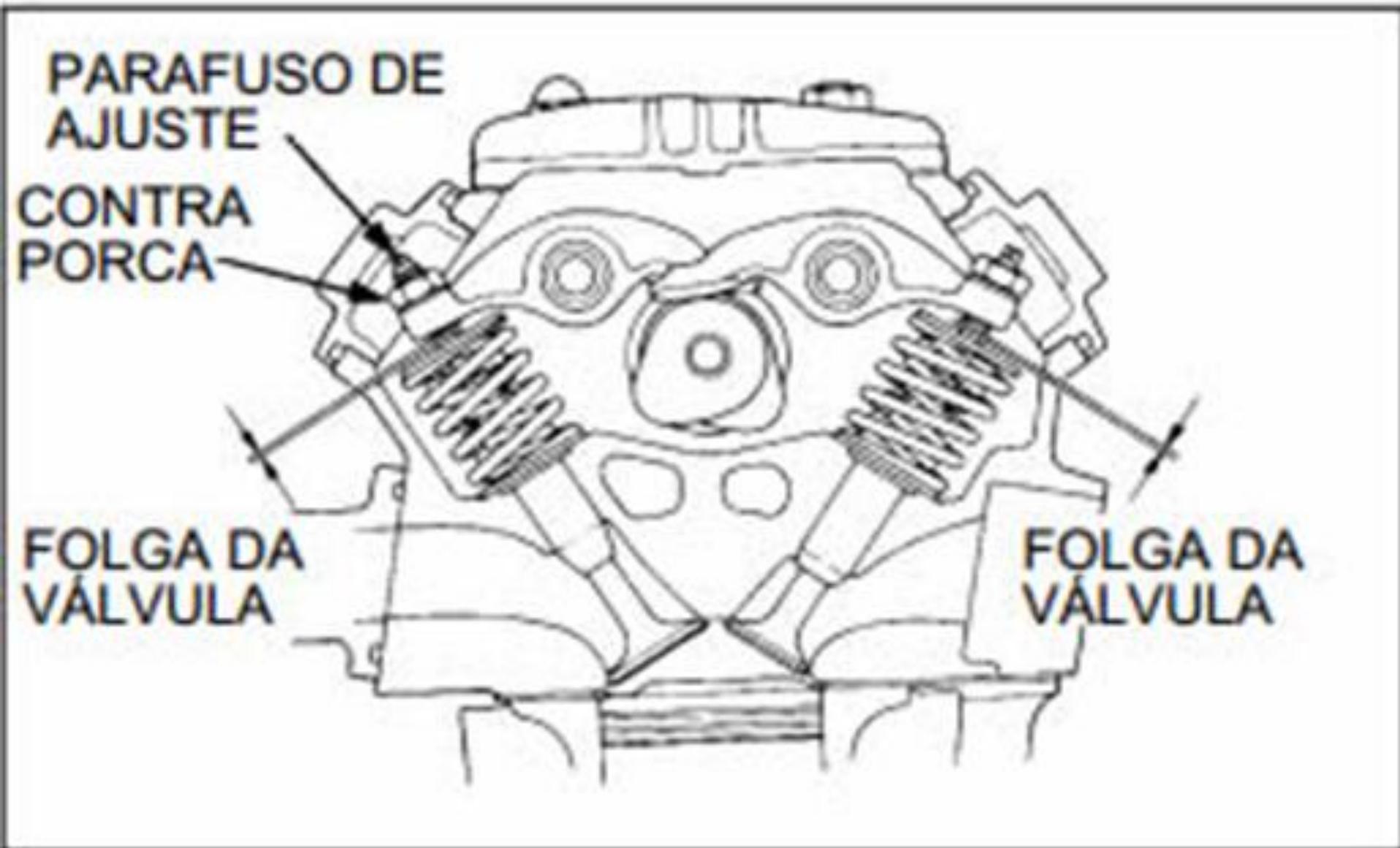
## ACIONAMENTO DAS VÁLVULAS POR MEIO DE HASTES IMPULSORAS, OU VARETAS





•ESQUEMA DE FUNCIONAMENTO DO SISTEMA DE ACIONAMENTO DAS VÁLVULAS







Seguidor de face plana



Seguidor com rolete

# Seguidor oscilante de face plana

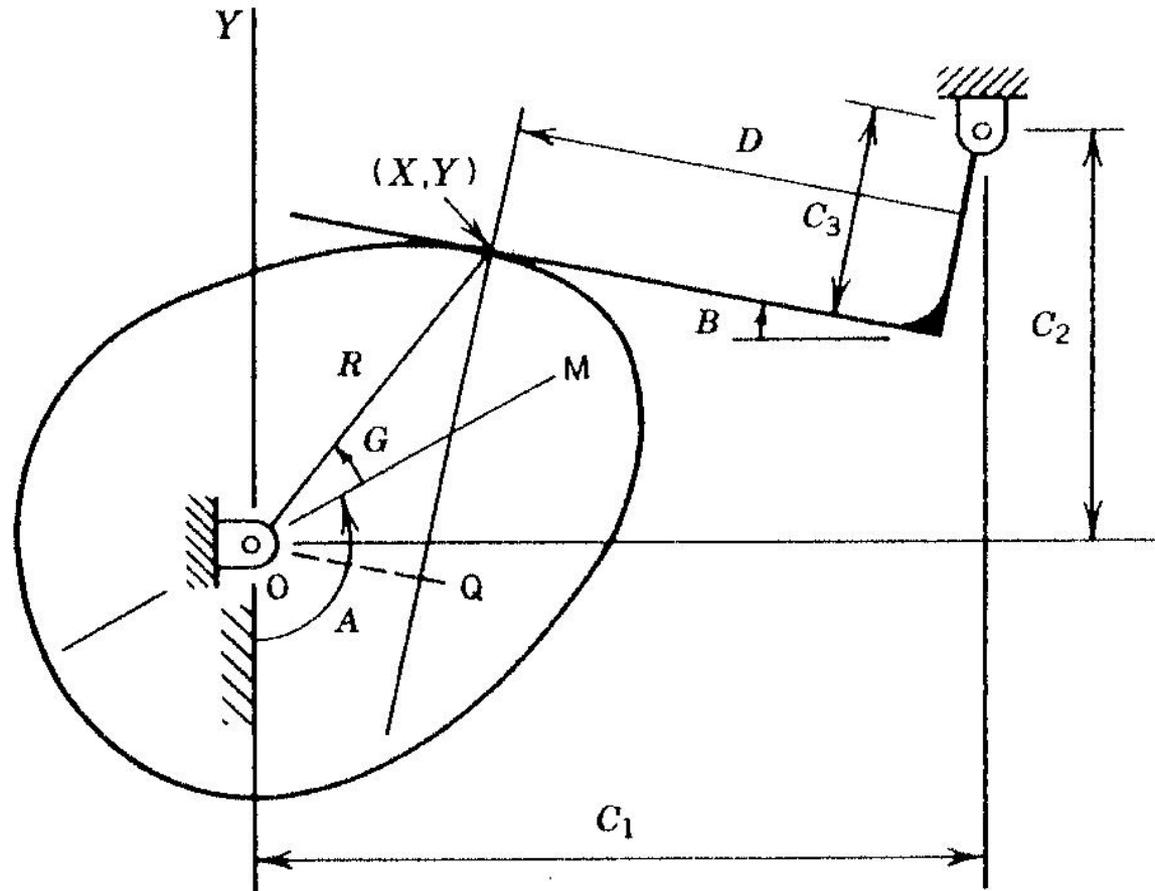


FIGURE 4.16 Cam With Pivoted, Flat-faced Follower

# Seguidor oscilante de face plana

$B(A)$  – ângulo do seguidor

$A$  – ângulo de posição da came

$$B(A) = B_0 + f(A)$$

$(R, G)$  – coordenadas polares do ponto de contato da came com o seguidor

$D$  – distância do ponto de contato sobre a face do seguidor

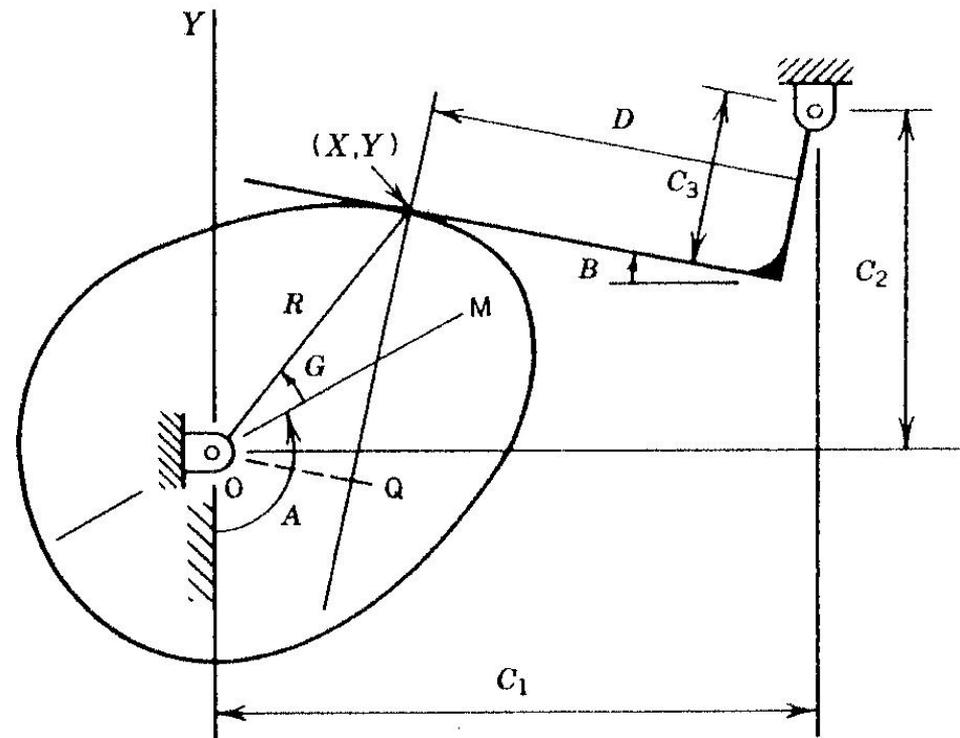


FIGURE 4.16 Cam With Pivoted, Flat-faced Follower

# Seguidor oscilante de face plana

Condição de contato permanente

$$\left. \begin{array}{l} V_f = \dot{B}.D \\ V_c = \dot{A}.\overline{OQ} \end{array} \right\} \Rightarrow \frac{\overline{OQ}}{D} = \frac{\dot{B}}{\dot{A}} = \frac{dB}{dA} = B'(A) = f'(A) \Rightarrow \overline{OQ} = D.f'(A)$$

$$\overline{OQ} + D + C_2.\sin(B) = C_1.\cos(B)$$

$$D = \frac{C_1.\cos(B) - C_2.\sin(B)}{1 + f'(A)}$$

Auxilia no cálculo do comprimento da face do seguidor

02/05/2019

Síntese de cames com seguidor oscilante

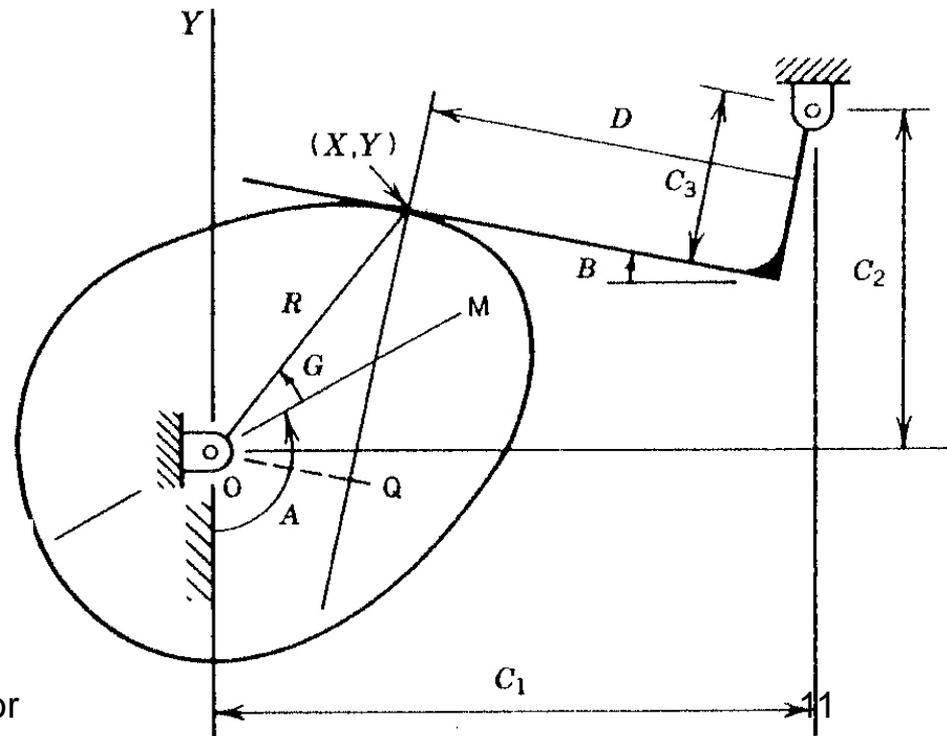


FIGURE 4.16 Cam With Pivoted, Flat-faced Follower

# Seguidor oscilante de face plana

Perfil da came

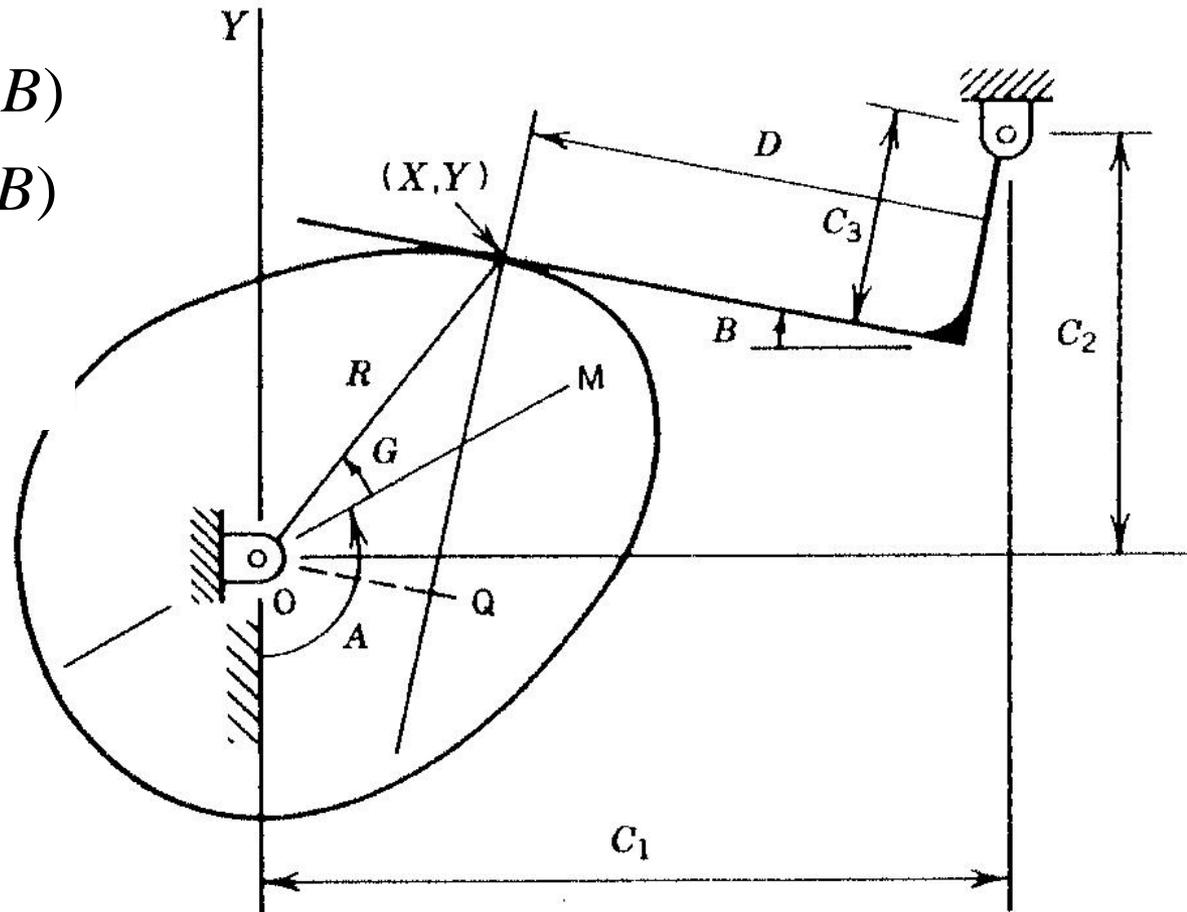
$$X = C_1 - C_3 \cdot \sin(B) - D \cdot \cos(B)$$

$$Y = C_2 - C_3 \cdot \cos(B) + D \cdot \sin(B)$$

$$A + G - \frac{\pi}{2} = \arctan_2\left(\frac{Y}{X}\right)$$

$$G = \frac{\pi}{2} - A + \arctan_2\left(\frac{Y}{X}\right)$$

$$R = \sqrt{X^2 + Y^2}$$



Cam With Pivoted, Flat-faced Follower

Coordenadas do perfil

A função  $\arctan_2$  está de volta!

# Seguidor oscilante de face plana

Perfil da came

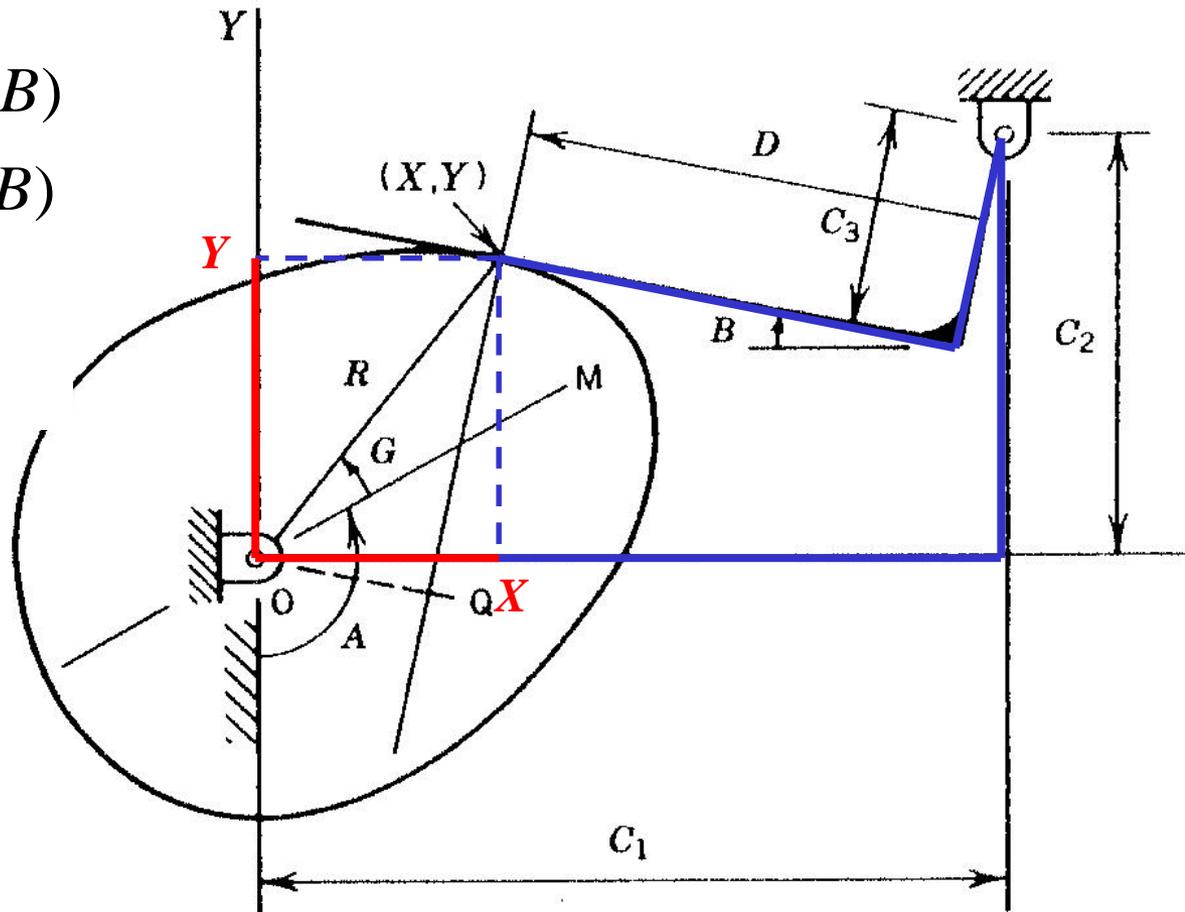
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Cam With Pivoted, Flat-faced Follower

Coordenadas do perfil  
A função  $\arctan_2$  está de volta!

# Seguidor oscilante de face plana

Tensões de contato

$$\sigma_0 = \sqrt{\frac{F \cdot E_1 \cdot E_2}{\pi \cdot t \cdot P \cdot (E_1 + E_2)}}$$

P – raio de curvatura no ponto de contato

$E_1, E_2$  – módulos de elasticidade (came e seguidor)

t – espessura

F – força de contato

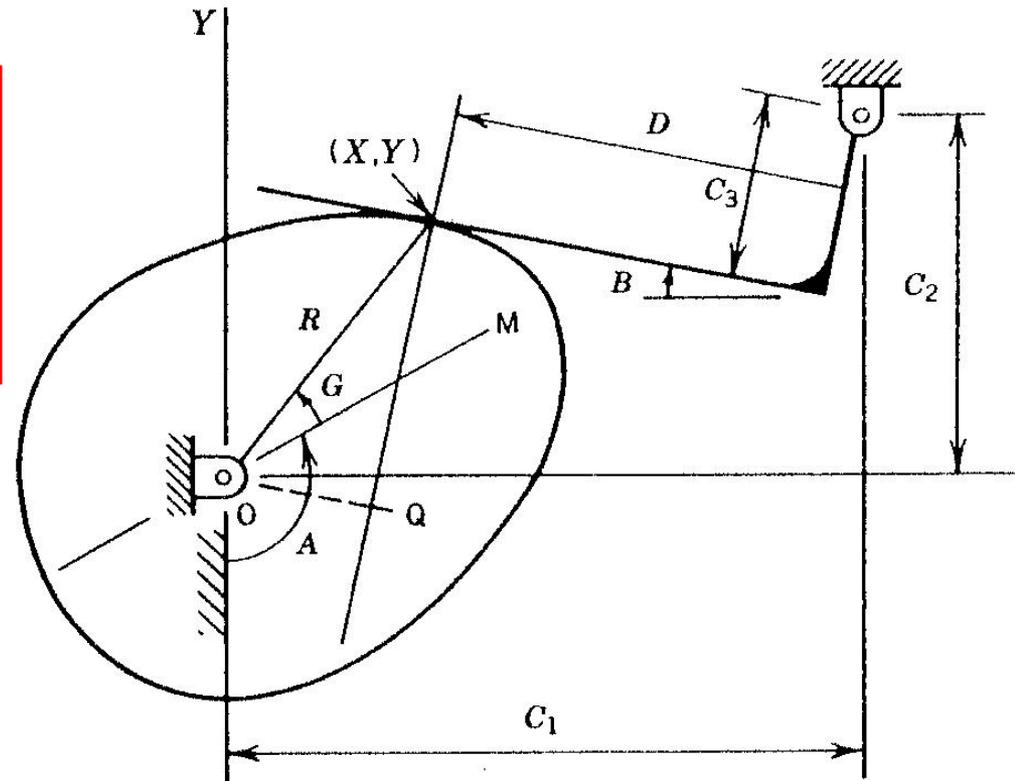


FIGURE 4.16 Cam With Pivoted, Flat-faced Follower



# Seguidor oscilante com rolete

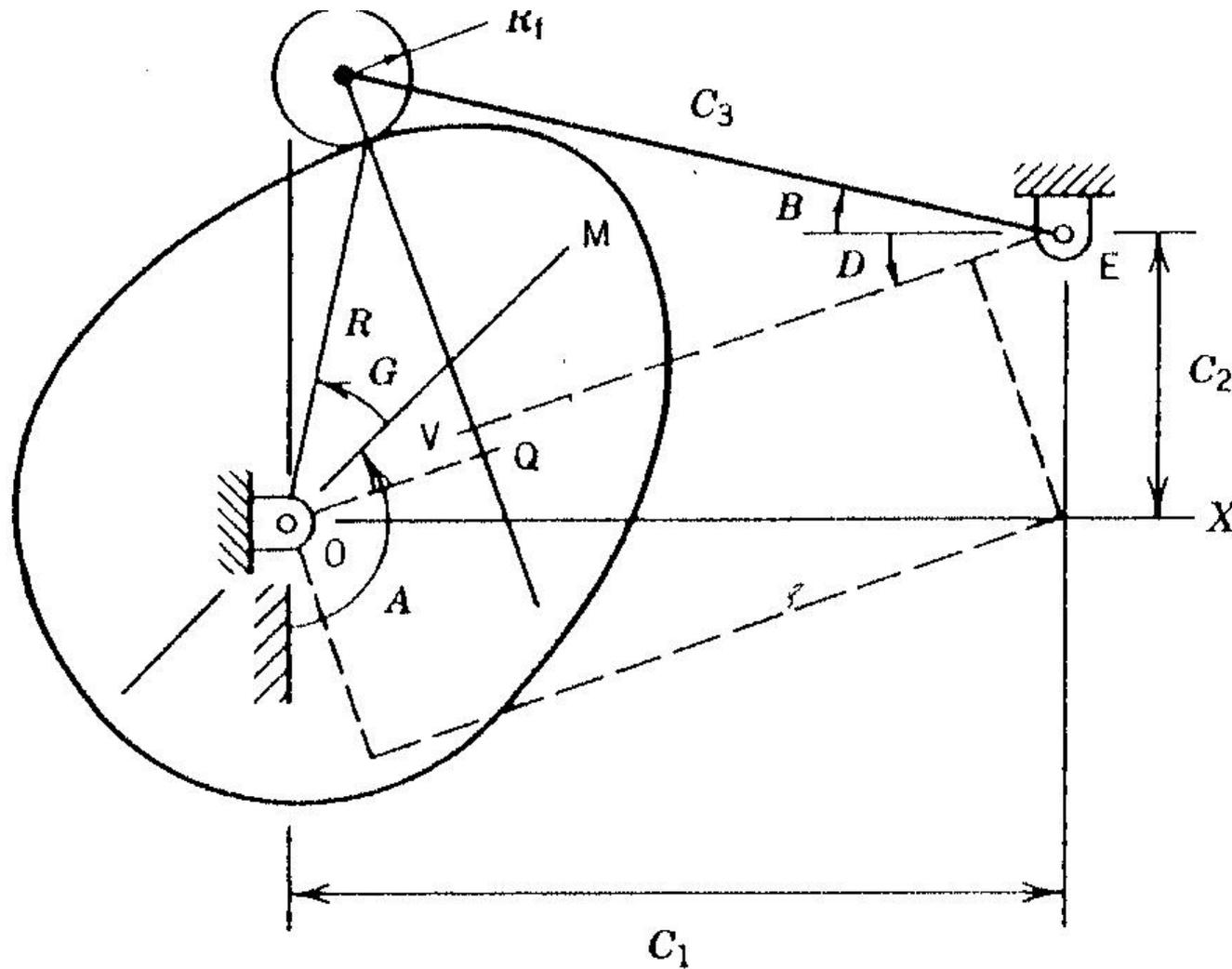


FIGURE 4.18 Cam With Pivoted Roller Follower

# Seguidor oscilante com rolete

Ângulo do seguidor

$$B(A) = B_0 + f(A)$$

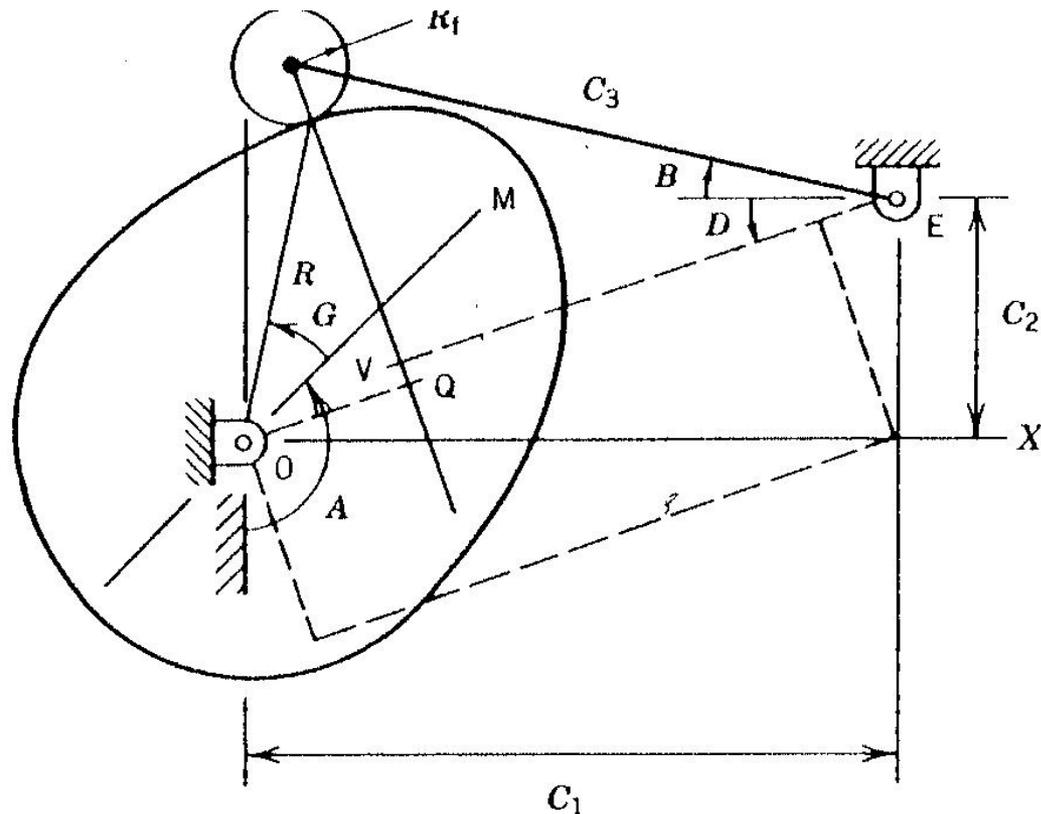


FIGURE 4.18 Cam With Pivoted Roller Follower

$B(A)$  – ângulo do seguidor

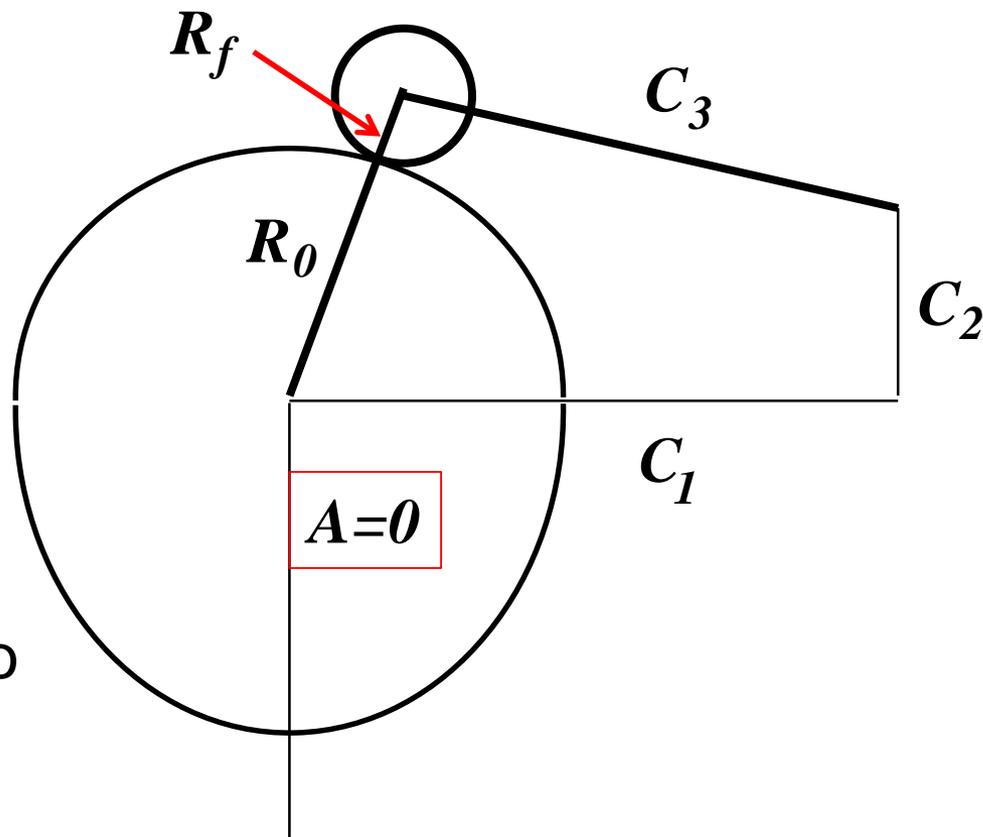
$A$  – ângulo de posição da came

$B_0$  – ângulo do seguidor para  $A=0$

# Seguidor oscilante com rolete

Ângulo do seguidor

$$B(A) = B_0 + f(A)$$



O valor de  $B_0$  pode ser obtido numericamente através da expressão:

$$(R_0 + R_f)^2 = (C_1 - C_3 \cdot \cos(B_0))^2 + (C_2 + C_3 \cdot \sin(B_0))^2$$

# Seguidor oscilante com rolete

Condição de contato permanente: orientação da linha de contato

$$\left. \begin{aligned} V_c &= \dot{A} \cdot \overline{OQ} \\ V_f &= \dot{B} \cdot \overline{VE} \end{aligned} \right\} \Rightarrow \dot{A} \cdot \overline{OQ} = \dot{B} \cdot \overline{VE}$$

$$\overline{OQ} = \frac{\dot{B}}{\dot{A}} \cdot \overline{VE}$$

$$\overline{OQ} = \frac{dB}{dA} \cdot \overline{VE}$$

$$\overline{OQ} = f' \cdot \overline{VE}$$

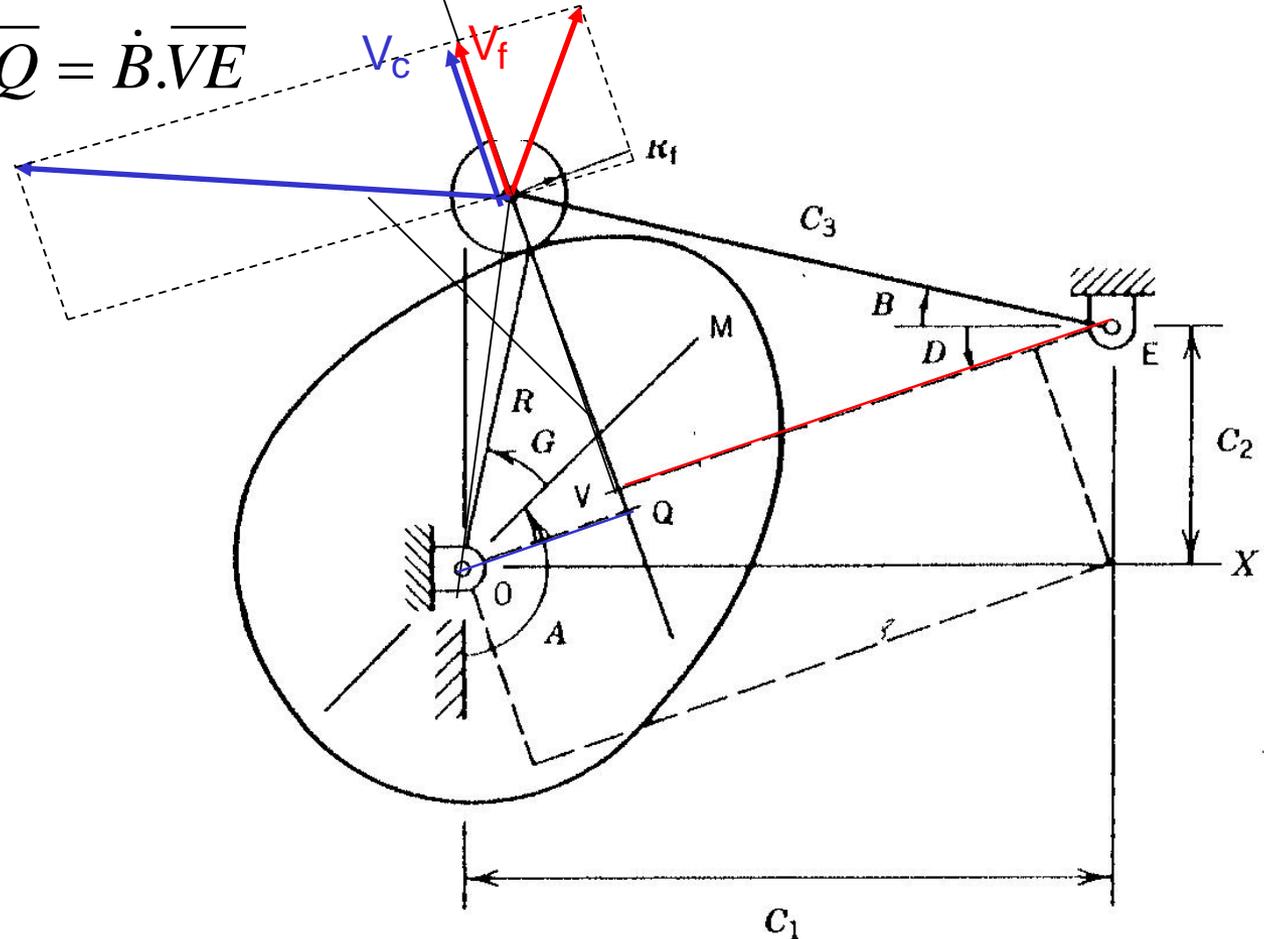


FIGURE 4.18 Cam With Pivoted Roller Follower

# Seguidor oscilante com rolete

Condição de contato permanente: orientação da linha de contato

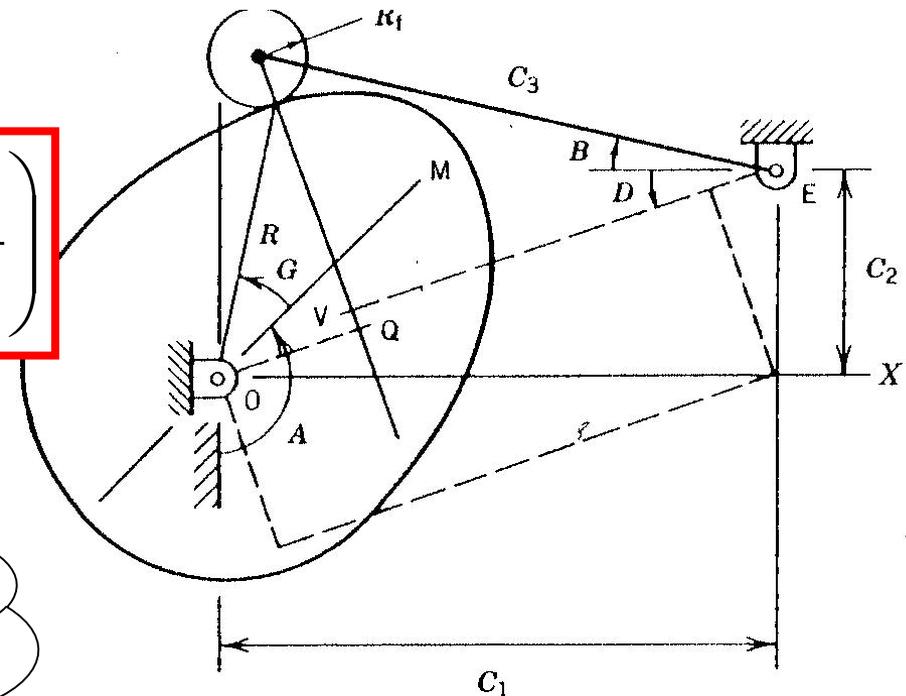
$$\overline{OQ} = f' \cdot \overline{VE}$$

$$\overline{VE} = C_3 \cdot \cos(B + D) = C_3 \cdot (\cos(B) \cdot \cos(D) - \sin(B) \cdot \sin(D))$$

$$\overline{OQ} + \overline{VE} = C_1 \cdot \cos(D) + C_2 \cdot \sin(D)$$

$$D = \arctan \left( \frac{C_3 \cdot (1 + f') \cdot \cos(B) - C_1}{C_3 \cdot (1 + f') \cdot \sin(B) + C_2} \right)$$

orientação da linha de contato



Cuidado para não confundir com a distância D do ponto de contato do seguidor de face plana!

02/05/2019

Síntese de cames com seguidor oscilante

FIGURE 10-10 Cam With Pivoted Roller Follower





# Seguidor oscilante com rolete

## Raio de curvatura no ponto de contato

$$R_c \cdot \sin(C) - P_p \cdot \sin(D) + C_3 \cdot \cos(B) - C_1 = 0$$

$$-R_c \cdot \cos(C) + P_p \cdot \cos(D) - C_3 \cdot \sin(B) - C_2 = 0$$

(ver desenvolvimento no livro)

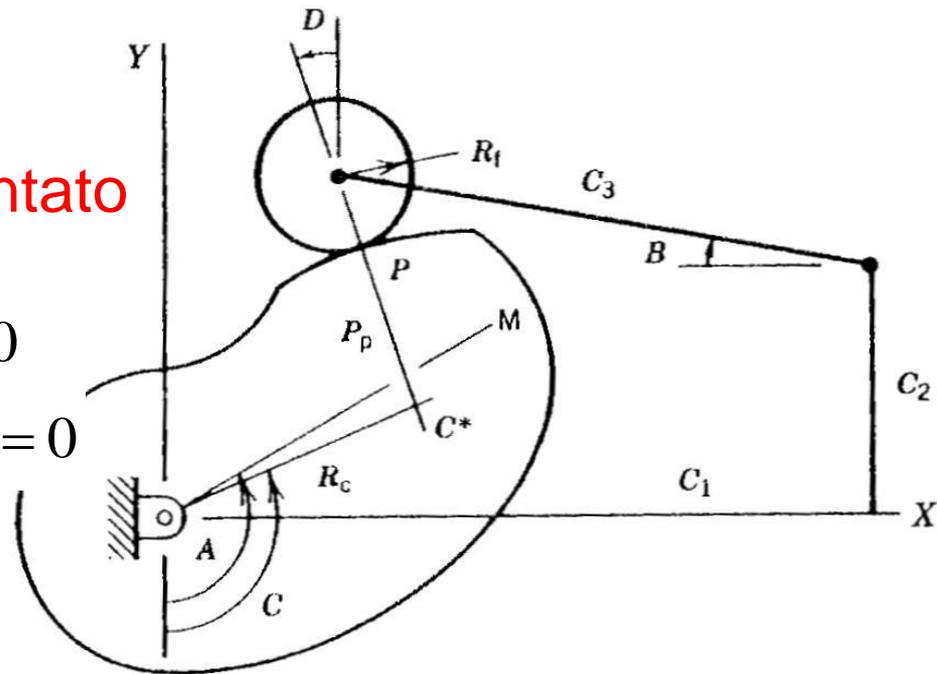


FIGURE 4.20 Radius of Curvature Determination

$$D' = \frac{C_3 \cdot f'' \cdot (C_2 \cdot \cos(B) + C_1 \cdot \sin(B)) - C_3^2 \cdot (1 + f')^2 + C_3 \cdot f' \cdot (1 + f') \cdot (C_1 \cdot \cos(B) - C_2 \cdot \sin(B))}{C_1^2 + C_2^2 + C_3^2 \cdot (1 + f')^2 + 2 \cdot C_3 \cdot (1 + f') \cdot (C_2 \cdot \sin(B) - C_1 \cdot \cos(B))}$$

$$P = \frac{C_2 + C_3 \cdot (1 + f') \cdot \sin(B)}{(1 - D') \cdot \cos(D)} - R_f$$

# Exercícios recomendados

Exercício 4.12

Exercício 4.19

4.12 For a particular cam with a pivoted, flat-faced follower, the follower rotational displacement is given by

$$f(A) = 0.08 [1 - \cos(2A/1.65)] \quad 0 \leq A < 1.65\pi$$
$$= 0.0 \quad 1.65\pi \leq A < 2\pi$$

The dimensional parameters are  $C_1 = 9.77$  in.,  $C_2 = 1.33$  in., and  $C_3 = 0.93$  in. The angle  $B_0$  is zero.

- Determine the minimum radius for the cam profile;
- For  $A = 1.23\pi$ , determine the polar coordinates for the contact point on the cam profile;
- For  $A = 1.23\pi$ , determine the radius of curvature for the contact point on the cam profile.

4.19 A cam with a pivoted, flat-faced follower is connected to a sliding link as shown. The angular displacement of the follower is given by

$$B(A) = B_0 + f(A)$$

where  $f(A)$  is the displacement function and  $B_0$  is the minimum rotation. The distance  $D$  and the angle  $C$  are known constants.

- Obtain an expression for the velocity coefficient,  $K_x = dX/dA$ , in terms of  $B_0$ ,  $C$ ,  $D$ ,  $f$ , and  $f'$ ;
- If the displacement function is

$$f(A) = 0.32 [1 - \cos(2\pi A/A_1)] \quad 0 \leq A < A_1$$

$$= 0.0 \quad A_1 \leq A < 2\pi$$

where

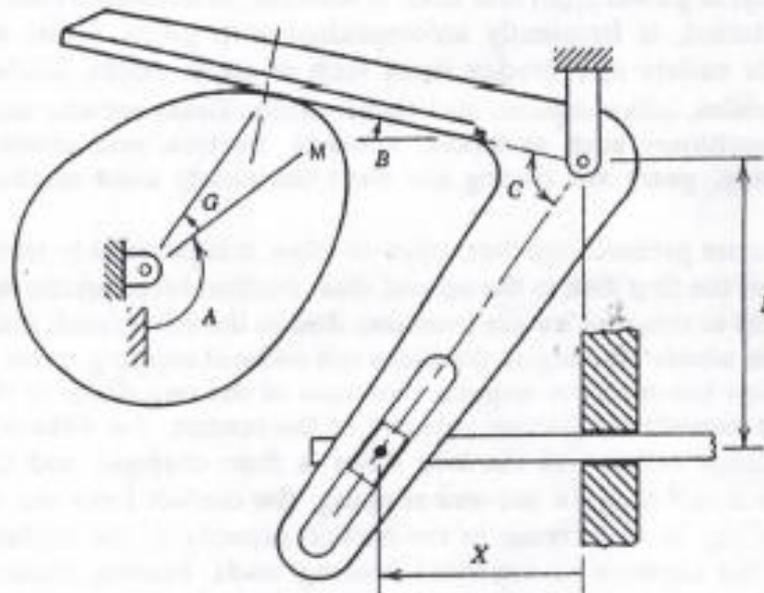
$$A_1 = 1.65\pi \text{ radians}$$

$$B_0 = 0.21 \text{ radians}$$

$$C = 1.02 \text{ radians}$$

$$D = 14.5 \text{ in.}$$

then, evaluate  $K_x$  for  $A = 1.22$  radians.



oscillante

# Dicas

## **Web-Based Mechanism Design and Analysis**

<http://www.softintegration.com/chhtml/toolkit/mechanism/>

## **APM Cam** (programa para projeto de cames)

<http://www.apm.ru/eng/products/apm/apmcameng>

# Referência

Doughty, S.. MECHANICS OF MACHINES. New York:  
John Wiley, 1988.

Capítulo 4